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# Isothermal section of the Dy-Cr-Ge system at 1073 K

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The phase equilibrium diagram of the Dy–Cr–Ge ternary system was constructed over the whole concentration range at 1073 K using methods of powder X-ray diffractometry, metallography, and electron microprobe analysis. Three ternary compounds are formed in the Dy-Cr-Ge system at the annealing temperature: Dy117Cr52Ge112 (Tb117Fe52Ge112 structure type, space group Fm-3m, a = 2.8723(8) nm), DyCr6Ge6 (SmMn6Sn6 structure type, space group P6/mmm, a = 0.51642(1), c = 0.82767(2) nm), DyCr1-xGe2 (CeNiSi2 structure type, space group Cmcm, a = 0.41249(5)-0.4140(3), b = 1.58287(2)-1.5890(7), c = 0.40048(5)-0.4001(2) nm). The DyCr1-xGe2 compound with CeNiSi2 structure type is characterized by a small homogeneity range limited by the DyCr0.28Ge2 and DyCr0.30Ge2 compositions. The solubility of chromium in the binary germanide Dy5Ge3 (Mn5Si3-type) extends up to 4 at. %. The DFT calculations were used to evaluate the thermodynamic, elastic and electrical properties of the DyCr1-xGe2 compound.

Keywords: Intermetallics; X-ray diffraction, phase equilibria, crystal structure.

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#### Introduction

The investigation of phase equilibria of the Dy-Cr-Ge system is part of a systematic study of the interaction between the components in ternary systems based on rare earth metals with 3*d*-elements and germanium to find new intermetallic compounds and study their physical properties To better understand the physical properties of intermetallics, the important step is to determine their relation of equilibrium with other phases and peculiarities of the crystal structure.

Among the ternary systems R-Cr-Ge (R is a rare earth metal), phase equilibrium diagrams are studied for R = Nd, Y, Gd, Er, and Tm [1-5]. Analysis of the literature data shows that the most studied compounds are RCr<sub>1-x</sub>Ge<sub>2</sub> (CeNiSi<sub>2</sub>-type) [6], RCr<sub>6</sub>Ge<sub>6</sub> (SmMn<sub>6</sub>Sn<sub>6</sub>-type) [7], and RCrGe<sub>3</sub> (BaNiO<sub>3</sub>-type) [8]. RCrGe<sub>3</sub> germanides (R = La-Nd, Sm) are characterized by ferromagnetic behavior with high Curie temperatures ranging from 60 to 155 K [8]. Detailed structural study of the RCr<sub>6</sub>Ge<sub>6</sub> compounds (R=Gd, Dy-Lu) shows that all studied compounds

revealed the off-stoichiometric composition [7]. Magnetic property measurements of RCr<sub>6</sub>Ge<sub>6</sub> germanides found magnetic ordering on TbCr<sub>6</sub>Ge<sub>6</sub>, DyCr<sub>6</sub>Ge<sub>6</sub>, and ErCr<sub>6</sub>Ge<sub>6</sub> [9, 10], TmCr<sub>6</sub>Ge<sub>6</sub> and LuCr<sub>6</sub>Ge<sub>6</sub> are paramagnets down to 2 K [7]. YbCr<sub>6</sub>Ge<sub>6</sub> germanide exhibits a magnetic transition at 3.4 K [7] with the ferrimagnetic ordering of the Cr and Yb sublattices. R<sub>117</sub>Cr<sub>52</sub>Ge<sub>112</sub> compounds with a giant unit cell (Tb<sub>117</sub>Fe<sub>52</sub>Ge<sub>112</sub>-type, *a*~2.9 nm) were found with R=Nd, Sm, and Gd [11, 12, 4]. The complexity of their crystal structure, which provides low thermal conductivity, is a basis for the creation of promising thermomagnetic materials.

In this contribution, we present experimental results from a study of the interaction between the components in the Dy-Cr-Ge system at 1073 K.

## I. Experimental methods

To construct the phase equilibrium diagram of the Dy-Cr-Ge system polycrystalline samples were synthesized by a direct arc-melting of the constituent components (metals were used in the form of ingots, with purity of dysprosium 99.9 wt.%; chromium, purity of 99.99 wt.%; and germanium, purity of 99.999 wt.%) under protected argon atmosphere (high purity Ti-gettered) on a watercooled copper bottom. The alloys were re-melted twice to provide better homogenization. The weight loss of the samples during the synthesis was less than 1 % of the initial total mass. Heat treatment of the produced alloys was performed in vacuum quartz ampoules at a temperature of 1073 K for 700 h. Then, the alloys were quenched in cold water without breaking the ampoules. The annealed samples were examined by X-ray diffractometry (DRON-4.0 diffractometer, radiation) to determine the phase composition. The observed diffraction intensities were compared with reference powder patterns of the binary phases, known ternary germanides, and pure elements (program PowderCell [13]). To control the chemical composition of the synthesized samples, determine the exact content of components in the phases, and confirm the phase composition, the method of energy-dispersive X-ray spectroscopy (EDRS) (electron microscope TESKAN VEGA 3 LMU, equipped by an X-ray analyzer with energy dispersive spectroscopy) was used. At least five measurements were taken to obtain the average value for each phase in each sample. For the crystal structure refinement, the diffraction data were collected at room temperature using STOE STADI P diffractometer (graphite monochromator, Cu  $K\alpha_1$  radiation). Rietveld refinement of the crystal structure was performed using the FullProf Suite program package [14].

The DFT calculations were performed using Vienna Ab initio Simulation Package VASP v.5.4.4 with PAW-type potentials [15]. The Perdew-Burke-Enzerhoff (PBE) exchange-correlation functional in the generalized gradient approximation (GGA) [16] with an 11×11×11 Monkhorst-Pack *k*-point set [17] was used in both cases. The semi-core 4*f*-electrons of Dy atoms were treated as core states. Optimized crystal structures were used for the final total energy calculations. Complete geometry relaxation (atomic positions and lattice parameters) was achieved by minimizing forces, stress tensor components, and total energies. The Bader charge density analysis was performed using the Bader v1.05 code [18].

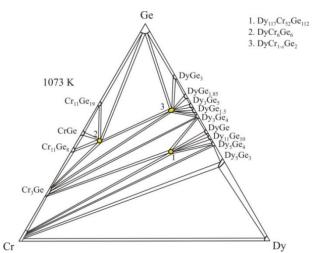
#### II. Experimental results

#### 2.1. Isothermal section of the Dy-Cr-Ge system

The data concerning the binary boundary Dy–Ge, Cr–Ge, and Dy–Cr systems were taken from the reported phase diagrams [19, 20]. No binary phases are formed in the Dy–Cr system. In the Cr–Ge system, four binary phases were confirmed at the temperature of annealing: Cr<sub>11</sub>Ge<sub>19</sub> (Mn<sub>11</sub>Si<sub>19</sub>-type), CrGe (FeSi-type), Cr<sub>11</sub>Ge<sub>8</sub> (Cr<sub>11</sub>Ge<sub>8</sub>-type), and Cr<sub>3</sub>Ge (Cr<sub>3</sub>Si-type). The Cr<sub>5</sub>Ge<sub>3</sub> binary with W<sub>5</sub>Si<sub>3</sub> structure type was not identified at the investigation temperature. According to the performed phase analysis, the sample at the corresponding composition contains two binary phases, Cr<sub>3</sub>Ge and Cr<sub>11</sub>Ge<sub>8</sub>, in equilibrium. As reported in the literature Cr<sub>5</sub>Ge<sub>3</sub> binary is stable at higher temperature, formed by

peritectic reaction at 1535 K and decomposes under the eutectoid reaction at 1269 K. Nine binary compounds were confirmed in the Dy-Ge system at 1073 K: DyGe<sub>3</sub> (DyGe<sub>3</sub>-type), DyGe<sub>1.85</sub> (DyGe<sub>1.85</sub>-type), Dy<sub>3</sub>Ge<sub>5</sub> (Y<sub>3</sub>Ge<sub>5</sub>-type), DyGe<sub>1.5</sub> (AlB<sub>2</sub>-type), Dy<sub>3</sub>Ge<sub>4</sub> (Er<sub>3</sub>Ge<sub>4</sub>-type), DyGe (TlJ-type), Dy<sub>11</sub>Ge<sub>10</sub> (Ho<sub>11</sub>Ge<sub>10</sub>-type), Dy<sub>5</sub>Ge<sub>4</sub> (Sm<sub>5</sub>Ge<sub>4</sub>-type), and Dy<sub>5</sub>Ge<sub>3</sub> (Mn<sub>5</sub>Si<sub>3</sub>-type).

To study the phase equilibria of the Dy-Cr-Ge ternary system, produced alloys were examined by X-ray diffractometry and energy dispersive X-ray spectroscopy. Based on the performed analysis, the isothermal section of the Dy-Cr-Ge system at 1073 K was constructed over the whole concentration range (Fig. 1). The Phase composition of individual alloys is presented in Table 1. Electron micrographs of some samples are shown in Fig. 2.



**Fig. 1.** Isothermal section of the Dy–Cr–Ge system at 1073 K.

At a temperature of 1073 K in the Dy–Cr–Ge system, the formation of two ternary compounds, DyCr<sub>6</sub>Ge<sub>6</sub> and DyCr<sub>1-x</sub>Ge<sub>2</sub>, was confirmed, and the formation of a new compound, Dy<sub>117</sub>Cr<sub>52</sub>Ge<sub>112</sub>, was identified. Analysis of the powder pattern of the sample with corresponding composition and the calculated lattice parameter (a = 2.8723(8) nm) indicated that the compound belongs to the Tb<sub>117</sub>Fe<sub>52</sub>Ge<sub>112</sub> (space group Fm–3m) structure type. Crystallographic characteristics of the ternary compounds from the Dy-Cr-Ge system are given in Table 2.

The solubility of Dy, Cr, and Ge in the binary compounds, except for Dy<sub>5</sub>Ge<sub>3</sub>, may be considered negligible (~1-2.5 at. %). The solubility of Cr in the Dy<sub>5</sub>Ge<sub>3</sub> binary germanide extends up to 4 at. % (a = 0.8416(2), c = 0.6261(5) nm for Dy<sub>5</sub>Ge<sub>3</sub>; a = 0.8432(2), c = 0.6288(2) nm for Dy<sub>63</sub>Cr<sub>4</sub>Ge<sub>33</sub> sample).

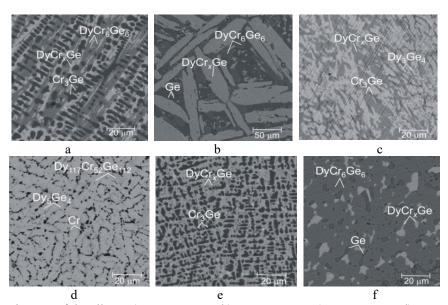
According to the data of the X-ray phase analysis, the  $DyCr_{1-x}Ge_2$  compound (CeNiSi<sub>2</sub>-type) is characterized by a small homogeneity range (x=0.7-0.72), which also includes the  $DyCr_{0.3}Ge_2$  composition reported in Ref. [6]. The crystal structure was calculated for the sample  $Dy_{31}Cr_9Ge_{60}$  (Fig. 3). Experimental details and refined atomic parameters are given in Tables 3, 4.

A detailed crystal structure study of the  $DyCr_6Ge_6$  compound was reported in our recent manuscript [7]. It was found that the  $DyCr_6Ge_6$  germanide crystallizes in the  $SmMn_6Sn_6$  structure type, a disordered variant of the

Table 1.

Phase composition	and FPMA da	ta for individual	samples of the D	v_Cr_Ge system
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Pnas	se composition ar	ia EPMA data io			•			. 0/
Composition, at. %	Phase	Structure type	Lattice parameters, nr		ĺ	EPMA data, at. %		
Composition, at. 70			а	b	С	Dy	Cr	Ge
Dy <sub>30</sub> Cr <sub>50</sub> Ge <sub>20</sub>	Dy <sub>5</sub> Ge <sub>3</sub>	Mn <sub>5</sub> Si <sub>3</sub>	0.8424(3)		0.6273(4)			
Dy30C130GC20	Dy <sub>5</sub> Ge <sub>4</sub>	Sm <sub>5</sub> Ge <sub>4</sub>	0.7586(3)	1.4563(5)	0.7676(4)			
	(Cr)	(W)	0.2892(3)					
Dy <sub>60</sub> Cr <sub>12</sub> Ge <sub>28</sub>	Dy <sub>5</sub> Ge <sub>3</sub>	Mn <sub>5</sub> Si <sub>3</sub>	0.8431(3)		0.6291(3)	62.51	3.78	33.71
Dy <sub>58,57</sub> Cr <sub>11,10</sub> Ge <sub>30,33</sub>	(Dy)	Mg	0.3592(3)		0.5654(3)	100.0		
Dy58,5/C111,10GC30,33	(Cr)	W		traces		100.0		
D C C-	Dy <sub>3</sub> Ge <sub>4</sub>	$Gd_3Ge_4$	0.4057(2)	1.0637(4)	1.4197(4)			
Dy <sub>15</sub> Cr <sub>55</sub> Ge <sub>30</sub>	Cr <sub>3</sub> Ge	Cr <sub>3</sub> Si	0.4627(3)					
	Dy <sub>117</sub> Cr <sub>52</sub> Ge <sub>112</sub>	Tb <sub>117</sub> Fe <sub>52</sub> Ge <sub>112</sub>	2.8724(6)					
Dy <sub>40</sub> Cr <sub>25</sub> Ge <sub>35</sub>	Dy <sub>5</sub> Ge <sub>4</sub>	Sm <sub>5</sub> Ge <sub>4</sub>	0.7588(3)	1.4543(4)	0.7678(4)	54.31	1.44	44.25
Dy <sub>42.43</sub> Cr <sub>33.53</sub> Ge <sub>35.04</sub>	Dy <sub>117</sub> Cr <sub>52</sub> Ge <sub>112</sub>	Tb <sub>117</sub> Fe <sub>52</sub> Ge <sub>112</sub>	2.8724(7)			42.76	18.16	39.08
•	(Cr)	(W)	0.2893(4)				100.0	
Dy <sub>10</sub> Cr <sub>50</sub> Ge <sub>40</sub>	DyCr <sub>6</sub> Ge <sub>6</sub>	SmMn <sub>6</sub> Sn <sub>6</sub>	0,5162(2)		0,8274(4)	7.99	46.55	45.46
Dy <sub>10.18</sub> Cr <sub>53.36</sub> Ge <sub>36.46</sub>	DyCr <sub>1-x</sub> Ge <sub>2</sub>	CeNiSi <sub>2</sub>	0.4139(3)	1.5900(7)	0.4001(1)	30.37	10.07	59.56
·	Cr <sub>3</sub> Ge	Cr <sub>3</sub> Si	0.4625(3)	` '		0.29	77.86	21.85
Dy <sub>15</sub> Cr <sub>40</sub> Ge <sub>45</sub>	DyCr <sub>x</sub> Ge <sub>2</sub>	CeNiSi <sub>2</sub>	0.4139(3)	1.5893(6)	0.4001(2)	30.22	9.67	60.11
Dy <sub>15.47</sub> Cr <sub>39.66</sub> Ge <sub>44.87</sub>	Cr <sub>3</sub> Ge	Cr <sub>3</sub> Si	0.4626(3)		` /	2.09	72.84	25.07
• • • • • • • • • • • • • • • • • • • •	Dy <sub>3</sub> Ge <sub>4</sub>	Gd <sub>3</sub> Ge <sub>4</sub>	0.4055(3)	1.0638(4)	1.4197(5)	42.61	0.08	57.31
Dy45Cr10Ge45	DyGe	TlI	0.4251(3)	1.0625(6)	0.3926(4)	51.44	0.15	48.41
Dy45.13Cr <sub>11.21</sub> Ge <sub>43.66</sub>	Dy <sub>11</sub> Ge <sub>10</sub>	Ho <sub>11</sub> Ge <sub>10</sub>	1.0869(4)		1.6351(5)	55.75	0.91	43.34
	Dy117Cr52Ge112	Tb <sub>117</sub> Fe <sub>52</sub> Ge <sub>112</sub>	2,8723(3)		` /	41.99	21.18	36.82
Dy <sub>7</sub> Cr <sub>46</sub> Ge <sub>47</sub>	DyCr <sub>6</sub> Ge <sub>6</sub>	SmMn <sub>6</sub> Sn <sub>6</sub>	0.5164(2)		0.8277(2)	8.27	46.08	45.65
Dy7.23Cr45.53Ge47.24	CrGe	FeSi	0.4796(3)		, , , , , , , , , , , , , , , , , , , ,		50.42	49.58
Dy40Cr10Ge50 Dy40.66Cr11.21Ge48.13	Dy <sub>3</sub> Ge <sub>4</sub>	Gd <sub>3</sub> Ge <sub>4</sub>	0.4056(2)	1.0638(4)	1.4197(4)	42.22	0.07	57.71
	Cr <sub>3</sub> Ge	Cr <sub>3</sub> Si	0.4628(3)	,		2.32	72.81	24.87
	Dy117Cr52Ge112	Tb <sub>117</sub> Fe <sub>52</sub> Ge <sub>112</sub>	2.8722(4)			41.22	21.36	37.42
	DyCr <sub>6</sub> Ge <sub>6</sub>	SmMn <sub>6</sub> Sn <sub>6</sub>	0.5164(3)		0.8276(4)	8.26	46.16	45.58
$Dy_{10}Cr_{40}Ge_{50}$	DyCr <sub>1-x</sub> Ge <sub>2</sub>	CeNiSi <sub>2</sub>	0.4136(2)	1.5890(6)	0.4001(1)	30,43	9,40	60,17
Dy9,19Cr42,76Ge48,05	(Ge)	C	0.5646(3)	1.0000(0)	01.001(1)	0.45	0.43	99.12
	DyCr <sub>x</sub> Ge <sub>2</sub>	CeNiSi <sub>2</sub>	0.4138(3)	1.5887(6)	0.4001(3)	32.07	9.01	59.92
Dy <sub>38</sub> Cr <sub>7</sub> Ge <sub>55</sub> Dy <sub>39.11</sub> Cr <sub>6.63</sub> Ge <sub>54.26</sub>	Dy <sub>3</sub> Ge <sub>4</sub>	Gd <sub>3</sub> Ge <sub>4</sub>	0.4054(3)	1.0638(5)	1.4196(4)	43.05	0.56	56.39
	Cr <sub>3</sub> Ge	Cr <sub>3</sub> Si	0.4625(4)	1.0030(3)	1.1170(1)	1.98	73.06	24.96
Dy <sub>35</sub> Cr <sub>5</sub> Ge <sub>60</sub>	DyCr <sub>1-x</sub> Ge <sub>2</sub>	CeNiSi <sub>2</sub>	0.4023(4)	1.5889(6)	0.4001(2)	1.70	, 5.00	2 1.70
	Dy <sub>3</sub> Ge <sub>4</sub>	Gd <sub>3</sub> Ge <sub>4</sub>	0.4057(2)	1.0639(5)	1.4195(4)			
	DyGe <sub>1,5</sub>	AlB <sub>2</sub>	0.3907(4)	1.0037(3)	0.4109(4)			
	DyCr <sub>6</sub> Ge <sub>6</sub>	SmMn <sub>6</sub> Sn <sub>6</sub>	0.5163(2)		0.4109(4)	8.52	46.10	45.38
Dy <sub>20</sub> Cr <sub>15</sub> Ge <sub>65</sub>	DyCr <sub>1-x</sub> Ge <sub>2</sub>	CeNiSi <sub>2</sub>	0.3103(2)	1.5886(3)	0.3999(4)	30.45	9.75	59.80
$Dy_{18.73}Cr_{16.12}Ge_{65,15}$	(Ge)	C	0.5648(3)	1.2000(3)	0.3777(4)	0.33	2.13	99.67
* * * * * * * * * * * * * * * * * * * *	(36)		0.50+0(5)	l	]	0.55	1	77.07

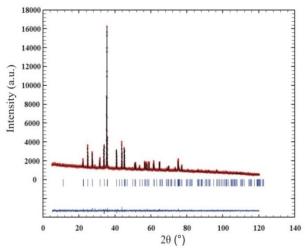


 $\begin{array}{c} \textbf{Fig. 2. SEM-images of the alloys: a)} \ Dy_{10}Cr_{50}Ge_{40}; \ b) \ Dy_{20}Cr_{15}Ge_{65}; \ c) \ Dy_{38}Cr_{7}Ge_{55}; \ d) \ Dy_{40}Cr_{25}Ge_{35}; \ e) \\ Dy_{15}Cr_{45}Ge_{40}; \ f) \ Dy_{10}Cr_{40}Ge_{50}. \end{array}$ 

Table 2.

Crystallographic characteristics of the ternary compounds from the Dy-Cr-Ge system

	0 1		<i>J</i>	J	J	
Compound	Space	Stanatura tura	Lattice parameters, nm			
Compound	group	Structure type	а	b	C	
DyCr <sub>6</sub> Ge <sub>6</sub>	P6/mmm	$SmMn_6Sn_6$	0.51642(	(1)	0.82767(2)	
DyCr <sub>1-x</sub> Ge <sub>2</sub>	C	C-Nic:	0.41249(	5)- 1.5828(2)-	0.40048(5)-	
	Стст	CeNiSi <sub>2</sub>	0.4140(	3) 1.5890(7)	c 0.82767(2)	
Dy <sub>117</sub> Cr <sub>52</sub> Ge <sub>112</sub>	Fm-3m	Tb <sub>117</sub> Fe <sub>52</sub> Ge <sub>112</sub>	2.8723(	8)		



**Fig. 3.** Experimental (circles), calculated (line) and difference (bottom line) X-ray patterns of the alloy Dy<sub>31</sub>Cr<sub>9</sub>Ge<sub>60</sub>.

MgFe<sub>6</sub>Ge<sub>6</sub>-type. The experimental study that was performed was also confirmed by DFT modeling. These data agree with previous investigations of the isotypic  $RCr_6Ge_6$  compound (R = Ho, Er, Y) studied by neutron diffraction [9].

#### 2.2. DFT modeling

The DFT modeling was performed for the hypothetical DyCr<sub>x</sub>Ge<sub>2</sub> solid solution  $(0 \le x \le 1)$ , which includes the experimentally observed ternary DyCr<sub>0.28</sub>Ge<sub>2</sub> compound. The symmetry of the crystal structure was reduced to introduce intermediate compositions (x = 0.25, 0.5, and 0.75). After geometry optimization, the corresponding enthalpies of mixing and formation were calculated, revealing that the formation of the continuous DyCr<sub>x</sub>Ge<sub>2</sub> solid solution  $(0 \le x \le 1)$  is energetically unfavorable (Fig. 4a). Despite the enthalpy of formation becomes less negative with increasing Cr content, the common tangent lines between DyGe<sub>2</sub> and DyCr<sub>6</sub>Ge<sub>6</sub> (ΔH<sub>f</sub> = -199 meV/atom [7]) reveal that the most stable composition is ~DyCr<sub>0.4</sub>Ge<sub>2</sub> with a narrow  $(0.4 \le x \le 0.45)$ homogeneity region and two-phase regions towards the DyGe<sub>2</sub> and DyCr<sub>6</sub>Ge<sub>6</sub> compounds.

The distribution of the density of electronic states of DyCr<sub>0.25</sub>Ge<sub>2</sub> (Fig. 4b) predicts its metallic behavior with the valence band formed predominantly by the s- and p-states of Ge and d-states of Cr. The Dy atoms contribute mainly to the density of states above the Fermi level (E<sub>F</sub>).

Table 3.

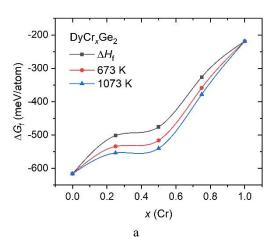
Experimental details and crystallographic data for DyCr<sub>0.28</sub>Ge<sub>2</sub> compound

Experimental details and crystallog	grapnic data for DyCr <sub>0.28</sub> Ge <sub>2</sub> compound
Alloy composition	Dy <sub>31</sub> Cr <sub>9</sub> Ge <sub>60</sub>
Refined composition	$DyCr_{0.28(5)}Ge_{2}$
Structure type	CeNiSi <sub>2</sub>
Pearson symbol	oS16
Space group, Z	Cmcm; 4
Unit cell parameters:	
a, nm	0.41249(7)
b, nm	1.58287(2)
c, nm	0.40048(5)
Cell volume $V$ , nm <sup>3</sup>	0.2615(1)
Calculated density $D_x$ , g/cm <sup>3</sup>	8.181
Diffractometer	STOE STADI P
Radiation, wavelength λ (nm)	Cu $K_{\alpha}$ , 1.54056
Angular range / increment (°2θ)	5.000≤2θ≤120.185/0.015
Reliability factors $R_{\text{Bragg}}$ , $R_{\text{f}}$	0.0439, 0.0551

Table 4.

Atomic coordinates and isotropic displacement parameters for DyCr<sub>0.28</sub>Ge<sub>2</sub>

The mid de et all and is ever epite displacement parameters for 2 j e10,28 e e2							
Атом	ПСТ	x	у	Z	Occupancy	$B_{iso}$ , Å <sup>2</sup>	
Dy	4 <i>c</i>	0	0.1036(2)	1/4	1	0.14(9)	
Cr	4 <i>c</i>	0	0.3048(9)	1/4	0.28(5)	1.52(1)	
Ge1	4 <i>c</i>	0	0.0506(7)	1/4	1	1.19(3)	
Ge2	4 <i>c</i>	0	0.7514(6)	1/4	1	1.79(3)	



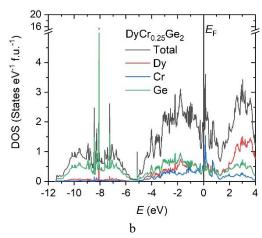


Fig. 4. Calculated energy of formation ( $\Delta G_f$ ) of the hypothetical solid solution DyCr<sub>x</sub>Ge<sub>2</sub> (a) and the distribution of the density of electronic states (DOS) (b) of DyCr<sub>0.25</sub>Ge<sub>2</sub>.

The calculated elastic properties of the  $DyCr_xGe_2$  solid solution showed that the crystal structure of  $DyCrGe_2$  is mechanically unstable. With the increasing Cr content, the bulk (B), Yung's (E), and shear (G) moduli change from 73.3, 106.2, and 42.2 GPa to 84.7, 64.0, and 23.3 GPa, respectively. Meanwhile, the Poisson's ratio increases from 0.259 (x=0) to 0.374 (x=0.75). Increasing Cr content leads to the almost linear rise of Pugh's B/G ratio from 1.738 to 3.638, indicating stronger ductile behavior and lower hardness. The corresponding Debye temperature decreases from 273.7 K (x=0) to 215.2 K (x=0.75).

#### **Conclusions**

An experimental study of the interaction of the components in the ternary system Dy-Cr-Ge in the whole concentration range at a temperature of 1073 K has confirmed the existence of ternary germanides DyCr<sub>6</sub>Ge<sub>6</sub> and DyCr<sub>1-x</sub>Ge<sub>2</sub> and the formation of a new ternary compound Dy<sub>117</sub>Cr<sub>52</sub>Ge<sub>112</sub> with a cubic structure of the Tb<sub>117</sub>Fe<sub>52</sub>Ge<sub>112</sub> type was established. Structural studies of the DyCr<sub>6</sub>Ge<sub>6</sub> compound proved that it belongs to the SmMn<sub>6</sub>Sn<sub>6</sub> structure type, a partially disordered variant of the MgFe<sub>6</sub>Ge<sub>6</sub>-type. It was established that the DyCr<sub>6</sub>Ge<sub>6</sub> and Dy<sub>117</sub>Cr<sub>52</sub>Ge<sub>112</sub> compounds are characterized by a point composition, germanide DyCr<sub>1-x</sub>Ge<sub>2</sub> with CeNiSi<sub>2</sub> structure type is characterized by a small homogeneity range, which is limited by the compositions DyCr<sub>0.28</sub>Ge<sub>2</sub> and DyCr<sub>0.30</sub>Ge<sub>2</sub>. Solubility of Cr in the Dy<sub>5</sub>Ge<sub>3</sub> binary (Mn<sub>5</sub>Si<sub>3</sub> structure type) extends up to 4 at. % of Cr. The calculated distribution of the density of electronic states of

DyCr<sub>0.25</sub>Ge<sub>2</sub> predicts its metallic behavior with the valence band formed predominantly by the s- and p-states of Ge and d-states of Cr. The thermodynamic modeling showed that the formation of the continuous DyCr<sub>x</sub>Ge<sub>2</sub> solid solution

 $(0 \le x \le 1)$  is energetically unfavorable, which is confirmed by the calculated elastic properties, and that the most stable composition is ~DyCr<sub>0.4</sub>Ge<sub>2</sub> with a narrow  $(0.4 \le x \le 0.45)$  homogeneity region and two-phase regions towards the DyGe<sub>2</sub> and DyCr<sub>6</sub>Ge<sub>6</sub> compounds.

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# Ізотермічний переріз діаграми стану системи Dy-Cr-Ge при 1073 К

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Методами рентгенофазового, рентгеноструктурного і рентгеноспектрального аналізів досліджено взаємодію компонентів та побудовано ізотермічний переріз діаграми стану потрійної системи Dy–Cr–Ge при 1073 К у повному концентраційному інтервалі. У системі Dy–Cr–Ge за температури відпалювання утворюються три тернарні сполуки: Dy117Cr52Ge112 (структурний тип  $Tb_{117}Fe52Ge112$ , просторова група Fm-3m, a=2,8723(8) нм), DyCr6Ge6 (структурний тип SmMn6Sn6, просторова група P6/mmm, a=0,51642(1), c=0,82767(2) нм), DyCr1-xGe2 (структурний тип CeNiSi2, просторова група Cmcm, a=0,41249(5)-0,4140(3), b=1,5828(2)-1,5890(7), c=0,40048(5)-0,4001(2) нм). Сполука DyCr1-xGe2 характеризується областю гомогенності, яка обмежена складами DyCr0,28Ge2 і DyCr0,30Ge2. Помітною розчинністю третього

Ключові слова: Інтерметалід; рентгенівська дифракція, фазові рівноваги, кристалічна структура.

DFT розрахунки виконано для оцінки еластичних і електричних властивостей сполуки DyCr<sub>x</sub>Ge<sub>2</sub>.

компонента характеризується германід DysGe3 (структурний тип MnsSi3), який розчиняє до 4 ат. % хрому.